An Empirical Investigation of the Italian Stock Market Based on the Four-Factor Pricing Model

Paola Brighi¹ and Stefano d Addona² This version: December 2004

Abstract:

Aim of this paper is to identify the pricing factor structure of Italian equity returns. The Italian Stock Market is characterized mainly by small quoted &rms. Small stocks have higher beta but beta di¤erences are not enough to explain returns di¤erences. We investigate how these di¤erences can be explained by other factors like size, value and momentum. A two step empirical analysis is provided where &rst we estimate an unrestricted three factor Model to test if there is any evidence of mispeci&cation. Secondly, we estimate the restricted model, with pricing errors equal to zero, through the Generalized Methods of Moments (GMM). Key &ndings of the paper can be classi&ed as follows:

1-The size premium for stocks shown in literature seems to be con&rmed for a domestic Italian investor, on the contrary the value premium appears to be statistically weakly dimerent from zero. Furthermore, augmenting the model with a momentum factor does not improve its performance.

2-Pricing errors appear to be not statistically di erent from zero in most of the analyzed portfolios, few exceptions are probably due to the small number of stocks composing them.

3-The GMM test of the Three Factors Model appears to support the Fama and French Model applied to the Italian Stock Market.

1 Introduction

In 1992 Fama and French (hereafter FF) published a landmark paper in which it is shown - with a cross-sectional analysis - strong evidence of explanatory power by size and book to market factors, compared with a little or no capacity by the beta to explain equity returns di¤erences. After them a large body of literature come out with evidence of little explanatory power by beta for explaining asset returns. Empirical works have mostly used US data and most of them reject beta and CAPM model (see, for example, Grinold, 1993).

In another paper, Fama and French (1993) - using a time-series approach - &nd basically the same evidence. Despite the fact that this model is a landmark

¹ University of Bologna - Department of Economics, Strada Maggiore 45, 40125 Bologna. e.mail: paola.brighi@unibo.it. Ph. +39 051 2092636, Fax. +39 051 2092664.

² University of Bologna - Department of Economics, Strada Maggiore 45, 40125 and

Columbia Business School -Doctoral Program-3022 Broadway, 311 Uris Hall New York, NY 10027. Email: sd2123@columbia.edu.

in the asset pricing theory little evidence has been published concerning international markets, with some exceptions for Japan (Chan et al., 1991, Daniel et al., 2001 and Charitou and Constantinidis, 2004) and UK (Fletcher, 1997, Strong and Xu, 1997, Gregory et al., 2001, Levis and Liodakis, 2001 and Daniel et al, 2004). Regarding small markets only recently a few papers have been published³. Concerning the Italian Stock Market some results have been recently produced on the empirical relevance of Fama and French three factors model (Aleati, Gottardo and Murgia, 2000 and Beltratti and Di Tria, 2002), on the source of momentum and contrarian strategies (Mengoli, 2004) and on the relation between equity returns and macroeconomic forces (Panetta, 2002). Following Fama and French (1993) we investigate the factor structure of the Italian Stock Market, through a GMM test of the Fama and French model augmented by a momentum exect from 1986 to 2004. Our empirical analysis shed further light on the relevance of di¤erent factors than beta - as size, book-to-market value and momentum exect - to explain equity returns dixerences. The paper is organized as follows: in section 2 we review the main theoretical and empirical contributions identifying the factor structure of equity returns. In section 3, we describe the data used for the empirical analysis and we explain the procedure adopted to construct the portfolios and the mimicking portfolios for the explanatory factors. Section 4 presents the results while section 5 concludes.

2 The theory of the factor structure determining equity returns

Even if the CAPM by Sharpe (1964), Lintner (1965) and Black (1972) (hereafter SLB) has been extensively studied and accepted, there is strong evidence in the literature rejecting its validity (see, for example, Grinold, 1993 and Fama and French, 1996b). Many attempts have been made to extend the one-factor model by SLB to multifactor models in order to explain better average returns. This approach is based on the empirical evidence that the intercept of the linear function of the CAPM is statistically di¤erent from zero: i.e. the beta does not explain alone the stock average returns.

The seminal work by Fama and French (1992) shows how the stock returns di¤erences are better explained by other factors than the market, as instead postulated by the classical theory of SLB. In particular, they &nd that the strongest consistency in explaining the average stock returns is represented by size and book-to-market value or equally the earning-price ratio, the cash-price ratio or the dividend-price ratio⁴. Unlike to the past literature on the Arbitrage

 ³ See, for example, L Her et al., 2004 for Canada; Asgharian and Hansoon, 2002 for Sweden; Di Iorio and Fa¤, 2000 and Fa¤, 2001 for Australia.
⁴ As suggested by Lakonishok, Shleifer and Vishny [1994, p. 1547] B/M is not a clean vari-

⁴ As suggested by Lakonishok, Shleifer and Vishny [1994, p. 1547] B/M is not a clean variable uniquely associated with economically interpretable characteristics of the &rms however they can be succesfully proxied by the market s expectations of future growth and the past growth of the &rms involved. The expected growth can be proxied by various measures of pro&tability to price that according to Gordon's formula are: dividend-to-price ratio (D/P),

Pricing Theory⁵, FF (1992) suggest that adding more factors than two does not improve the estimates obtained by their model on stock returns⁶. However, after FF some authors &nd evidence in favour of a third pricing factor known as the momentum factor (see, for example, Jegadeesh and Titman, 1993). Coherently with our econometric investigation in the next two subsections we review the main theoretical and empirical works on the di¤erent pricing factors as size, book-to-market value and momentum in a national asset pricing perspective.

2.1 Literature review

2.1.1 Theoretical models

The FF thesis As discussed in FF (1992) some critics to the standard SLB model emergerd just in the eighties: for example, Banz (1981) shows that the &rm size improves the estimation of the stock average return; Bhandari (1988) notes a positive relation between the &rm leverage and the stock average return; Stattman (1980) and Roseberg, Reid and Lanstein (1985) &nd that the U.S. stock average returns are positively linked to the book-market value ratio; Basu (1983) shows that the earning-price ratio improves the estimation of the U.S. stock cross-section average returns when in the statistical test it is considered the &rm size and the market $^-$ at the same time.

What FF (1992) add to the previous literature is the joint role of market ⁻, size, earning-price ratio, leverage and book-to-market ratio with reference to NYSE, AMEX and NASDAQ stock returns. In their seminal work they show that the SLB model does not work in the U.S. market for the all period between 1941-1990. In particular, they show that the univariate relation between average return and size, leverage, E/P, and book-to-market equity are strong. In multivariate tests, the negative relation between size and average returns is robust to the inclusion of other variables. The positive relation between book-

See Ross, 1976, Roll and Ross, 1980, Chen et al., 1986 and Asprem, 1989.

⁶ In a augmented FF model augmented by macro factors - as industrial production growth, consumer prices, both expected and unexpected, risk premiums, interest term structure, the federal funds rate, housing starts, the producer index and an idiosyncratic return proxy - Merville et al. (2001) &nd that the most signi&cant factors for an individual common stock can be associated to: i) the market return - beta; ii) the market capitalization - size; and iii) the investment opportunity set - value. Higher-order factors can be uniquely associated with macroeconomic variables that, however, add little explanatory power to the standard three FF model.

cash-to-price ratio (C/P) and earning-to-price ratio (E/P). An alternative way to classify stocks is based on past growth rather than on expectations of future growth. In this case past growth is measured by growth in sales since sales is less volatile than either cash ! ow or earnings. The above analysis supported empirically by Lakonishok, Shleifer and Vishny [1994] and by Fama and French [1998] implies that to estimate stocks value we can choose among our regressors indi ¤erently the ratios B/M, D/P, E/P and C/P. This is the reason why - without any loss of generality - in our following econometric analysis we use the ratio E/P instead of B/M. Another way to proxy the B/M ratio is through the Tobin s Q, which is in turn a measure of future investment opportunities. We thank an anonimous referee to have helped us to clarify this point.

to-market equity and average returns also persists in competition with other variables.

Moreover, FF (1992) show that even if the size factor has attracted more attention among the researchers the book-to-market equity has a consistently stronger role in average returns.

The FF (1992) analysis & nally implies that, &rst the SLB market $\bar{}$ is not so useful to understand the cross-section of average stock returns in U.S. and second the combination of size and book-to-market equity seems to absorb the roles of leverage and E/P in average stock returns. In other terms, the main conclusion of FF (1992) is that stock risks are multidimensional: one dimension of risk is proxied by size, the other one is proxied by the ratio of the book value of common equity to its market value. In this way FF (1992) confute the role of $\bar{}$ in the explanation of the stock returns; in other terms if there is a role for $\bar{}$ in average returns, it has to be found in a multi-factor model.

Critics to FF model Even if the pioneer works by FF (FF, 1992 and FF, 1993) have given origin to a new and rich stream of the literature their results are not immune by critics. Critics (see, for example, De Bondt and Thaler [1985], Lakonishok, Shleifer and Vishny [1994], Haugen, [1995], MacKinlay [1995] and Knez and Ready [1997]) are mainly based on the observation that the violations of the SLB model are not simply linked to missing risk factors as in FF but to the existence of market imperfections, to the presence of irrational investors and to the inclusion of biases in the empirical methodology.

On the one hand, De Bondt and Thaler [1985], Lakonishok, Shleifer and Vishny [1994] and Haugen, [1995] argue that the so called value strategies - small market capitalization and high book-to-market equity stocks - yield higher returns than glamour strategies - large market capitalization and low book-to-market equity stock - because of investor overreaction rather than compensation for risk bearing. They argue that investors systematically overreact to recent corporate news, unrealistically extrapolating high or low growth into the future. This, in turn, leads to underpricing of value and the overpricing of glamour stocks. The value strategies produce higher returns because these strategies exploit the suboptimal behavior of the typical investor and not because these strategies are fundamentally riskier.

Unlike to FF, Lakonishok, Shleifer and Vishny [1994] with reference to the US stock market (NYSE and AMEX) from April 1968 to April 1990 &nd little support for the view that value strategies are fundamentally riskier than glamour strategies.

So the reason of the controversy is not the fact that value strategies perform better than glamour strategies - on which there is some consensus at the least with reference to US markets⁷ - but the reason of why this happens. According to Lakonishok, Shleifer and Vishny [1994] the reason has to be found in the

 $^{^{7}}$ In fact concerning the Italian Stock Market the value premium does not hold at all for the entire period considered (January 1980-April 2002). See section 5.

irrational behavior of investors⁸.

On the other hand, MacKinlay [1995] and Knez and Ready [1997] base their arguments on the empirical methodology. MacKinlay [1995] evaluates the plausibility of multifactors models à la FF using ex ante analysis instead of ex post analysis. They show that, ex ante, CAPM deviations due to missing risk factors will be very di¢cult to be empirically detected, whereas deviations resulting from nonrisk-based sources are easily detectable. They &nally conclude that multifactor pricing models alone do not entirely resolve CAPM deviations. The empirical test of the FF multifactor model conducted by Knez and Ready [1997] suggest that the size exect is completely driven by sample extreme observations that represent less than 1% of each month s data. The Least Trimmed Squares (LTS) regression used instead of the OLS regression of FF implies that most small &rms actually do worse than larger &rms. In fact, the LTS regression implies a positive relation between &rm size and average return that is exactly the opposite of what FF obtained in their study. The result obtained by Knez and Ready [1997] is particularly relevant for the Italian Stock Market formed for most by small &rms. However, further empirical analysis would be useful to accept such a result as an economic regularity rather than a sampling error. Concerning this point many authors (see, for example, Ferson, Sarkissian and Simin [1999]) cautions against using empirical regularities as explanatory risk factors . One way to test the empirical validity of FF three factors model is to use international data.

International factors An extension of the multifactors model to an international framework is advanced by Fama and French [1998]. They argue that an international CAPM à la SLB cannot explain the di¤erence between value stock returns and glamour stock returns. After having observed that there is evidence of an existing value premium in twelve markets outside the U.S. during the 1975-1995 period, FF (1998) show that an international three-factor model that includes a risk factor for relative distress seems to capture the value premiun in the returns for major markets. This result holds also for emerging markets.

However, they do not compare the world factor model to country-speci&c models. Gri¢n (2002) compares the world factor model to country speci&c models and &nds that the domestic models explain more time-series variation and generally provide more accurate pricing than the world model. Moreover, he does not &nd any bene&ts from the extension of the FF three factors model to a global context. Even if from a statistical point of view the world model seems more signi&cant than a country model, from an economic point of view it implies a small increase in explanatory power. In fact, the country-speci&c three model has lower in-sample and out-of-sample pricing errors than models that include foreign factors. In summary, there are no bene&ts to extending the three-factor model to an international context⁹.

⁸ For further developments on this point see, for example, Shefrin [2001].

⁹ For more developments on the international multifactos models see, among others, Kora-

The momentum exect TO BE COMPLETED

2.1.2 Empirical models

The cross-section approach TO BE COMPLETED

The time-series approach TO BE COMPLETED

3 Data and methodology

The aim of this section is to test the Fama and French Three Factor Model [FF, 1992 and FF, 1993] on the Italian Stock Market. As anticipated in the previous section FF found a strong evidence of capacity in explaining cross sectional [FF, 1992] and time series [FF, 1993] asset returns by variables as the &rms size and the book-to-market ratio.

The Fama and French model can be expressed as follows:

[1] $E(ExR_i) = [E(ExRm) + [E(SMB) + d_iE(HML)];$

where:

 $ExRm = excess return on market portfolio, (R_m i R_f);$

SMB (Small Minus Big) = the return on the mimicking portfolio for the size factor;

HML (High Minus Low) = the return on the mimicking portfolio for the book-to-market factor;

 R_f = return on a risk-free asset.

To test this model it is necessary to estimate the following equation:

[2]
$$R_{itj} R_{ft} = {}^{\textcircled{R}}_{i} + {}^{-}_{i} (R_{mtj} R_{ft}) + {}^{\circ}_{i} (SMB_{t}) + {}^{\pm}_{i} (HML_{t}) + {}^{"}_{it}$$

To estimate the above equation we perform a two step test:

i) First we test the unrestricted model with the classical OLS method for &nding the consistence of the model and if the pricing errors (alpha) are not signi&cantly dimerent from zero. In fact, comparing the equations [1] and [2], it appears obvious that the model has one important implication: the intercept term (alpha) in a time-series regression should be zero that means the alpha of

jczyk and Viallet (1989), Bansal, Hsieh and Viswanathan (1993), Stulz (1995),

the model is equal to the pricing error. Given this implication we use the Black, Jensen and Scholes [1972] approach for evaluating this assumption: basically we run a time-series regression for each asset to be tested and then we use the standard OLS t-statistics for testing if the pricing errors (alpha) are zero.

ii) After this empirical analysis we use the Generalized Methods of Moments (GMM) to test the resticted (alpha=0) FF Model. The GMM framework allows us to avoid the assumption that the asset returns are normally distributed and temporarily i.i.d. The basic idea of GMM procedure is to choose the parameters to be estimated so as to match the moments of the model itself with the empirical moments of the data. The main advantage of GMM procedure is that the statistical assuptions required are very weak.

The resticted model to be estimated is:

[3]
$$R_{itj} R_{ft} = \frac{1}{i} (R_{mtj} R_{ft}) + \frac{1}{i} (SMB_t) + \frac{1}{i} (HML_t) + \frac{1}{it} [i = 1:::N]$$

with 4N sample moment condition for each portfolio and 3N parameters to be estimated. We can test the N over-identifying restrictions using the GMM-statistic that is the minimized value of the objective function.

We compute the GMM-statistic as:

[4]
$$GMM = m(\mu)^{"}S^{i}^{1}m(\mu)$$

where:

 $m(\mu) = empirical vector of moment conditions;$

S = weighting matrix used for estimating the parameters.

Under the null hypothesis that the overidentifying restrictions are satis&ed, the GMM-statistic times the number of regression observations is asymptotically \hat{A}^2 with degrees of freedom equal to the number of overidentifying restrictions. Finally for calculating the standard errors of our estimated parametrs we use the Newey and West [1987] variance-covariance estimator.

3.1 Data

The data used for testing the Three Factors Model are derived from the close price of the entire Italian Stock Market for the period between the 1-jan-1980 and 1-Apr-2002. The total number of assets included is 587 and the frequency is monthly. We included 287 stock from MIBTEL Index, 45 stocks from NUMTEL Index and 255 stock from the DEAD-STOCKS Index¹⁰ for avoiding possible survivor biases¹¹. The source is Datastream.

We compute the return on a single asset as:

[5] $r_t = \frac{p_{t_i} p_{t_i}}{p_{t_i}} + dy_t$

¹⁰ The list of dead stocks is provided by Datastream.

¹¹See Banz and Breen (1986) and Fama and French (1998).

where:

 $p_t = price at time t;$

 dy_t = estimated monthly dividend yield at time t.

In order to estimate the monthly dividend yields, we spread the correspondent annual dividend yields supplied by Datastream so that, compounding the monthly dividends gives back exactly the annual dividends. The risk-free asset used in our empirical tests is the 1-months ITL Euro-Currency.

3.2 Risk factors

In order to obtain the mimicking portfolios for the factors, we construct three groups of assets based on Size tertiles and 3 groups of assets based on the Price-Earnings ratio (P/E) tertiles. By the intersection of these groups we obtain 9 portfolios named as R1V, R2V, R3V, R1M, R2M, R3M, R1G, R2G, R3G; where for example R3G is the portfolio containing the &rms with an high P/E ratio (growth &rms) and a high Market Value (big &rms). On those portfolios we calculate the value weighted returns. Each portfolios is rebalanced every year¹².

The next step is to construct the risk factors:

i) Market Factor (MKT): index constructed by calculating the value weighted return of all the assets listed. The risk factor is calculated by subtracting the risk free rate¹³.

ii) Size Factor (SMB): mimicking portfolio constructed by calculating the di¤erence between the simple mean of the returns on the small &rms portfolios and the return on the big &rms portfolios:

[6]
$$SMB_t = \frac{P}{i=V;M;G} \frac{1}{3}Ri1_t i \frac{P}{i=V;M;G} \frac{1}{3}Ri3_t:$$

iii) P/E Factor (HML): mimicking portfolio constructed by calculating the di¤erence between the simple mean of the returns on the value &rms portfolios and the return on the growth &rms portfolios¹⁴:

[7]
$$HML_t = \frac{\mathbf{P}_1}{\mathbf{P}_1^3} RiV_t \mathbf{i} \quad \frac{\mathbf{P}_1}{\mathbf{P}_1^3} RiG_t:$$

Last step before starting the empirical tests is to construct the portfolios of which the returns has to be explained in the Three Factors Model. To obtain the

¹² Due to lack of data the &rst available period for constructing all the tertiles is 1-jan-1986.

¹³ To con&rm the correctness of our methodology we calculate the correlation between the Market Factor and the Morgan Stanley Capital International Index (MSCI ITALY). The result is more than comforting: 98% on the entire sample period.

 $^{^{14}}$ We use the Price-Earning ratio (P/E) instead of the Book-to-Market ratio used by Fama and French for two main reason. First of all our choice is due to the avaiability of the data for the Italian Market; second because the P/E ratio is well accepted in literature as proxy to identify a &rm as a value or as a growth &rm. See also footnote 5.

dependent variables of our time-series regression we construct sixteen portfolios based on value-growth ranking and on size ranking of the &rms.

If we identify two distinct set of assets as GV (four groups of assets based on P/E ratio quartiles) and SZ (four groups of assets based on Market Value quartiles), we can obtain, from the intersection of GV and SZ, sixteen portofolios and we can calculate the value weighted returns as the returns calculated for the mimicking portfolios (see above in this section).

4 Results

4.1 Summary statistics

The whole sample period is January 1986-September 2004. As expected, table 1 shows that the correlations between the three factors are low and in two cases are not statistically di¤erent from zero¹⁵. This result is consitent with the FF model and allows us in using the three series for testing the model.

[Insert table 1]

As the table 2 shows, all the mimicking portfolios series show a consistent evidence of non normality in the monthly returns. This is consistent with a well known literature (see for example Fama [1965, 1976] or Blattemberg and Gonedes [1974]).

[Insert table 2]

This evidence suggests to use a GMM framework for testing the restricted model. Generally speaking all the constructed portfolios show annualized returns statistically signi&cant¹⁶, and, going deeper in our analysis, is possible to show some characteristics of the Italian Market. As shown in the table 2, the annualized return on the size mimicking portfolio (SMB) is about 13% with a 20% of volatility and appears to be statistically signi&cant. This is consistent with the theory of a risk premium for the small &rms.

 $^{^{15}}$ A simple method to test the null hypothesis that the product moment correlation coeC-cient is zero can be obtained using Student s t-test on the t statistic:

 T_{i} stat = $\frac{\sqrt{N_{i}-2}}{1_{i}}$;

where N is the number of observations.

Under the null hypothesis that the correlation between the two variables is not signi&cantly di¤erent from zero, the t-statistic is distribuited as a Student s t with N₁ 2 degrees of freedom. ¹⁶ In this case for testing the null hypothesis that the returns are signi&cantly di¤erent from zero we use the classical t-statistic. Under the null hypothesis that the return is equal to zero the t-statistic is distribuited as a Student s t with N degrees of freedom.

On the contrary the annualized return of the value-growth mimicking portfolio (HML) is about 7,5% with a volatility of 18% and it appears to be statistically weakly di¤erent from zero.

Finally the annual excess return of the Market index (MKT) is about 11% with a volatility of about 26% and, hence, consistent with the assumption of risk aversion¹⁷.

4.2 Econometric results

Table 3A and 3B report the results for the OLS analysis to test if the pricing errors (alpha) are di¤erent from zero. In &ftheen portfolios the intercept term is not statistically signi&cant. Looking at the classical OLS statistics, we cannot reject the null hypothesis (5% con&dence level) of alpha=0 only in portfolio R44. In this case the composition of the portofolio is based on only few assets for the &rst observations due to lack of data. This characteristic can lead the model to be rejected because, in practice, we are testing with the same regression two totally di¤erent assets : a single stock in the beginning of the sample and a diversi&ed portfolio in the remaining period.

[Insert tables 3A & 3B].

Table 4A and 4B report the results for the GMM analysis to test the Three Factors Model developed by FF applied to the Italian Stock Market. The results seem to support the model; we &nd an R² range between 0.39 for the R14 portfolio and 0.89 for the portfolio R44 and, in nine out of 16 portfolios, the model cannot be rejected, as the p-values of the GMM statistics show, with a 5% of con&dence level. We reject the null hypothesis that the overidentifying restrictions are satis&ed in seven out of 16 portfolios: R12, R21, R32, R33, R41, R43 and R44.

[Insert tables 4A & 4B]

To understand the motivation behind the rejection of the null hypothesis in seven out of 16 portfolios, we investigate if there are other factors that can be used in the model to explain portfolio returns. In order to do that &rst of all we estimate the unrestricted model (see equation 2) with a GMM procedure to investigate if the model is characterized by some pricing errors¹⁸.

[Insert Table 5]

 $^{^{17}}$ Considering the sample period 1-jan-1986 to 1-apr-2002, the t-stat. of the annual excess return on the market index is 1,77 and seems to be statistically weakly di¤erent from zero. But, on the other hand, if we consider the entire sample period, from 1-jan-1980 to 1-apr-2002, we &nd an annual excess return of 17% with a volatility of about 27% and a t-stat. of 2,56.

¹⁸ In this case we use GMM procedure for estimating the unrestricted model for avoiding possible biases given by the distribution assumption.

4.2.1 The momentum exect

Then we try to estimate a model with other mimicking factors. To investigate if there is some momentum exect in the Italian Market as in other stock markets (see Rouwenhorst [1998]) we construct another mimicking portfolio based on the dixerence between the stock with the highest past years average returns and the stock with the lowest past years average returns.

In practice we construct three groups of assets based on size tertiles and 3 groups of assets based on the past year s returns tertiles. By the intersection of these groups we obtain 9 portfolios named as R1W, R2W, R3W, R1WL, R2WL, R3WL, R1LS, R2LS, R3LS; where for example R3W is the portfolio containing the winners with a high Market Value.

The mimicking portfolio associated to the momentum factor WML (Winner Minus Loser) is constructed by calculating the di¤erence between the simple mean of the returns on the winners portfolios and the return on the losers portfolios:

[8] WML_t =
$$\frac{\mathbf{P}}{_{i=1}^{1}} \frac{1}{_{3}} RiW_{t} i = \frac{1}{_{3}^{3}} RiLS_{t}$$
:

The annualized return on the momentum mimicking portfolio (WML) is about -1,5% and appears to be statistically non di¤erent from zero. This is an evidence of absence of momentum e¤ect in the Italian Stock Market. However the correlation with the other factors (SMB, HML and MKT) is respectively 0.07, 0.03 and 0.09 and is never statistically signi&cant.

The new restricted model to be estimated is:

[9]
$$R_{iti} R_{ft} = \bar{i} (R_{mti} R_{ft}) + \hat{i} (SMB_t) + \pm i (HML_t) + \hat{i} (WML_t) +$$

"it [i = 1:::N]

with 5N sample moment condition for each portfolio and 4N parameters to be estimated. Hence we get again N over-identifying restrictions.

Table 6 reports the results for the GMM analysis of the restricted model with the momentum mimicking factor. The results are pretty clear: we reject the null hypothesis that the overidentifying restrictions are satis&ed in all the portfolios for the model with the momentum factor. It seems possible to conclude that there is no momentum exect in the Italian Stock Market.

[Insert table 6]

5 Conclusions

The key &ndings of our work can be summarized as follows. The size premium is con&rmed for a domestic Italian investor while the value premium is statistically weakly dimerent from zero for the Italian Market. Then the pricing errors appears to be not dimerent from zero in most of the portfolios; when they are not it is probably due to the composition of the portolios that, being formed by only

few assets at the beggining, may present a bigger variance of the disturbance term that can a ect the model speci&cation.

Then the GMM test of the Three Factors Model appears to support the FF Model applied to the Italian Stock Market with an R^2 range between 0.39 and 0.89. In nine out of 16 portofolios the GMM-statistics show a p-value that lead us to conclude that the null hypothesis that the overidentifying restrictions are satis&ed, cannot be rejected.

Finally we investigate if there is some evidence of momentum exect but we have found no evidence of it on the Italian Stock Market.

Further research could come from the inclusion in the model of other explaining factors. In particular it could be interesting to investigate how the anomaly of an high risk free rate during 80 s in Italy as well as others factors related with the yield curve can explain the italian stock returns. Further developments can also derive from the inclusion in the model of the exhange-rate risk.

6 References

TO BE COMPLETED

Asprem, 1989

Bansal, R., D. Hsieh, and R.Viswanathan, A New Approach to International Arbitrage Pricing, Journal of Finance, 48, 1719-1747, 1993

Banz, Rolf W, The Relationship between return and market value of common stocks, Journal of Financial Economics, 9, 3-18, 1981

Banz, R., and W. Breen, Sample dependent results using accounting and market data: Some evidence, Journal of Finance, 41, 779-793, 1986

Basu, S., The relationship between earnings yield, market value, and return for NYSE common stocks: Further evidence, Journal of Financial Economics, 12, 129-156, 1983

Bhandari, L.C., Debt/Equity ratio and expected common stock returns: Empirical evidence, Journal of Finance, 43, 507-528, 1988

Black F., M. Jensen and M. Scholes , The Capital Asset Pricing Model: some empirical tests in Jensen M. Studies in the theory of capital markets Praeger, New York, 1972.

Blattberg R. and N. Gonedes N. A comparison of the stable and student distributions as statistical models of stock prices Journal of Business, 47, 244-280, 1974.

Chan, L.K., Y. Hamao and J. Lakonishok, Fundamentals and Stocks Returns in Japan, Journal of Finance, vol. 46 (December), pp. 1467-84, 1991

Charitou A. and E. Constantinidis, Size and Book-to-Market Factors in Earnings and Stock Returns: Empirical Evidence for Japan, Illinois International Accounting Summer Conferences Working Paper, 2004

Daniel, K., S. Titman and K.C. Wei HJ., Explaining the Cross-Section of STock REturns in Japan factors or Characteristics , Journal of Finance, Vol LVI, n. 2, 2001

Daniel ChiHsiou Hung, Mark Shackleton1 and Xinzhong Xu CAPM, Higher Comoment and Factor Models of UK Stock Returns Journal of Business Finance & Accounting Volume 31 Issue 1-2 Page 87 - January 2004

Davis J. The cross section of realised stock returns: the pre-COMPUSTAT evidence Journal of Finance, 49/5, 1579-1593, 1994

Di Iorio, A. and R. Fa¤, Foreign Exchange Exposure and Pricing in the Australian Equities Market: A Fama and French Framework, mimeo, 2001

Douglas Foster, F., T. Smith and R. E. Whaley, Assessing Goodness-of-Fit of Asset Pricing Models: The Distribution of the Maximal R^2 , The Journal of Finance, 52/2, 591-607, 1997

De Bondt, W. and R. Thaler, Does the stock market overreact , Journal of Finance, 40, 793-805, 1985

Fama E., The behaviour of stock market prices Journal of Business, 38, 34-105, 1965.

Fama E. and K. French, The cross-section of expected stock returns Journal of Finance, 47/2, 427-465, 1992.

Fama E. and K. French, Common risk factors in the returns of stocks and bonds, Journal of Financial Economics, 33, 3-56, 1993.

Fama E. and French, Size and book-to-market factors in earnings and returns, Journal of Finance, 50/1, 131-155, 1995.

Fama E. and K. French, Multifactor explanations of asset pricing anomalies , Journal of Finance, 51/1, 55-84, 1996a.

Fama E. and K. French, The CAPM is Wanted, Dead or Alive , Journal of Finance, 51/5, 1947-1958, 1996b.

Fama E. and K. French, Value versus growth: the international evidence, Journal of Finance, 53/6, 1975-1999, 1998.

Fama E. and K. French, The Equity Premium , The Journal of Finance, 57/2, 637-659, 2002

Fama, E. F. and J. D. MacBeth, Risk, Return, and Equilibrium: Empirical Tests, The Journal of Political Economy, 81/3, 607-636, 1973

Fletcher, J. (2000), On the Conditional Relationship between Beta and Return in International Stock Returns, International Review of Financial Analysis, Vol. 9, pp. 23545.

Ferson, W.E., S. Sarkissian, and T. Simin, The Alpha Factor Asset Pricing Model: A Parable, Journal of Financial Markets, 2, 49-68,1999

Gregory, A., R.D.F. Harris and M. Michou (2001), An Analysis of Contrarian Investment Strategies in the UK, Journal of Business Finance & Accounting, Vol. 28, Nos. 9 & 10 (Nov/Dec), pp. 1193-228.

Gri&n, J. M., Are the Fama and French Factors Global or Country Speci&c?, The Review of Financial Studies, 15/3, 783-803, 2002

Grinold R. Is beta dead again? , Financial Analysts Journal , 49, 28-34, 1993

Hansen L. Large sample properties of generalized methods of moments estimators , Econometrica , 50, 1029-1054, 1982.

Hansen L. and K. Singleton, Generalized instrumental variables estimation of non linear rational expectations models, Econometrica, 50, 1269-1286, 1982.

Haugen, R., The New Finance: The Case against ECcient Markets , Prentice Hall, Englewood Ckixs, N.J.,1995

Knez, P. J. and M. J. Ready, On the Robustness of Size and Book-to-Market in Cross-Sectional Regressions, The Journal of Finance, 52/4, 1355-1382, 1997

Korajczyk, R.A., and C.J. Viallet, An Empirical Investigation of International Asset Pricing, Review of Financial Studies, 2, 553-585, 1989

Lakonishok, J., A. Shleifer and R. W. Vishny, Contrarian Investment, Extrapolation, and Risk, The Journal of Finance, 49/5, 1541-1578, 1994

Levis, M. and M. Liodakis (2001), Contrarian Strategies and Investor Expectations: The U.K. Evidence , Financial Analysts Journal, Vol. 57, No. 5 (Sept/Oct), pp. 43-56.

MacKinlay A.C. and M. Richardson, Using generalized methods of moments to test mean-variace e¢ciency, Journal of Finance, 46, 511-527, 1991.

MacKinlay A.C., Multifactor models do not explain deviations from the CAPM , Journal of Financial Economics, 38, 3-28, 1995

Merville, L. J., S. Hayes-Yelsken and Y. Xu, Identifying the Factor Structure of Equity Returns, The Journal of Portfolio Management, 2001, 51-61

Newey W. and K. West, A simple positive de&nite, heteroskedasticity and autocorrelation consistent covariance matrix, Econometrica, 55, 703-705, 1987.

Roseberg, B., K. Reid and R. Lanstein, Persuasive evidence of market ine¢ciency, Journal of Portfolio Management 11, 9-17, 1985

Rouwenhorst, K.G, International Momentum Strategies , Journal of Finance 53/1, 267-284, 1998.

Shefrin, H. (ed. by), Behavioral &nance , Cheltenham, Northampton, E. Elgar, 2001

Stattman, D., Book values and stock returns , The Chicago MBA: A Journal of Selected Papers 4, 25-45, 1980

Strong N. and X. Xu, Explaining the Cross-section of UK Expected Stock Returns, British Accounting Review 29, 1-23, 1997

Stulz, R.M., International Asset Pricing: An Integrative Survey , in R. Jarrow, V. Maksimovic, and W.T. Ziemba (eds.), The Handbook of Modern Finance, North Holland, Amsterdam, 1995.

| Table 1: Correlation m | - | | |
|------------------------|--------------|---------------|------------|
| Correlation | SMB | HML | MKT |
| SMB | 1.0000 | 0.3196 | -0.0598 |
| HML | 0.3196 | 1.0000 | 0.0337 |
| MKT | -0.0598 | 0.0337 | 1.0000 |
| t-stat | | | |
| SMB-HML | 4.699 | | |
| SMB-MKT | -0.835 | | |
| HML-MKT | 0.469 | | |
| N | lonthly data | a 1-jan-86 to | 1-apr-2002 |

| Table 2: Basic descriptive statistics | | | | | | | | |
|---------------------------------------|--------------|-------------|------------|--|--|--|--|--|
| | SMB | HML | MKTRF | | | | | |
| Mean | 0.0109 | 0.0060 | 0.0090 | | | | | |
| Median | 0.0076 | 0.0010 | -0.0039 | | | | | |
| Maximum | 0.3741 | 0.4178 | 0.2747 | | | | | |
| Minimum | -0.1272 | -0.2685 | -0.1618 | | | | | |
| Std. Dev. | 0.0577 | 0.0517 | 0.0743 | | | | | |
| Skewness | 1.5781 | 2.0697 | 0.7072 | | | | | |
| Kurtosis | 11.0095 | 26.4809 | 4.0580 | | | | | |
| | | | | | | | | |
| Jarque-Bera | 599.0821 | 4595.2510 | 25.3497 | | | | | |
| Probability | 0.0000 | 0.0000 | 0.0000 | | | | | |
| | | | | | | | | |
| Annualized return | 0.1383 | 0.0740 | 0.1136 | | | | | |
| Annualized volatility | 0.2000 | 0.1790 | 0.2575 | | | | | |
| t-stat | 2.7810 | 1.6631 | 1.7733 | | | | | |
| Μ | lonthly data | 1-apr-86 to | 1-apr-2002 | | | | | |

| Table 3A: OLS | Test of unrest | ricted Fama | and French | Model | | | | | | |
|----------------|----------------|-------------|-------------|--------|-----------------|-------------|--------|-----------|-------------|---------|
| Dependent Vari | able: R11 | | | | Dependent Varia | ble: R13 | | | | |
| | | | | | | | | | | |
| | Coefficient | | t-Statistic | | | Coefficient | | | t-Statistic | |
| SMB | 0.3519 | 0.0703 | | 0.0000 | SMB | 0.2236 | | 0.0733 | | 0.0030 |
| HML | 0.2119 | 0.0785 | 2.7000 | 0.0080 | HML | -0.1127 | | 0.0818 | -1.3800 | 0.1700 |
| MKT | 0.7737 | 0.0517 | 14.9700 | 0.0000 | MKT | 0.8675 | | 0.0538 | 16.1100 | 0.0000 |
| CONS | 0.0019 | 0.0039 | 0.4800 | 0.6330 | CONS | 0.0066 | | 0.0041 | 1.6200 | 0.1080 |
| F(3,188) | 88.3100 | | | | F(3,177) | 87.7100 | | | | |
| Prob > F | 0.0000 | | | | Prob > F | 0.0000 | | | | |
| R-squared | 0.5824 | | | | R-squared | 0.5807 | | | | |
| Adj R-squared | 0.5758 | | | | Adj R-squared | 0.5741 | | | | |
| Auj N-Squaleu | 0.5756 | | | | Auj K-Squareu | 0.5741 | | | | |
| Dependent Vari | able: R12 | | | | Dependent Varia | ble: R14 | | | | |
| | Coefficient | Std. Error | t-Statistic | Prob. | | Coefficient | Std. | Error | t-Statistic | Prob. |
| SMB | 0.3831 | 0.0701 | 5.4700 | 0.0000 | SMB | 0.5783 | | 0.0941 | 6.1500 | 0.0000 |
| HML | 0.0804 | | | 0.3050 | HML | -0.2759 | | 0.1050 | | |
| MKT | 0.7944 | | | | MKT | 0.6695 | | 0.0691 | | 0.0000 |
| CONS | -0.0026 | 0.0039 | -0.6700 | | CONS | 0.0035 | | 0.0053 | | 0.6380 |
| CONS | -0.0026 | 0.0039 | -0.0700 | 0.0000 | 00113 | 0.0025 | | 0.0053 | 0.4700 | 0.0300 |
| F(3,188) | 89.6200 | | | | F(3,188) | 41.2000 | | | | |
| Prob > F | 0.0000 | | | | Prob > F | 0.0000 | | | | |
| R-squared | 0.5859 | | | | R-squared | 0.3941 | | | | |
| Adj R-squared | 0.5794 | | | | Adj R-squared | 0.3846 | | | | |
| Auj N-Squareu | 0.5794 | | | | Auj K-Squareu | 0.5640 | | | | |
| Dependent Vari | able: R21 | | | | Dependent Varia | ble: R23 | | | | |
| | Coefficient | Std. Error | t-Statistic | Prob. | | Coefficient | Std. | Error | t-Statistic | Prob. |
| SMB | 0.4035 | 0.0581 | 6.9400 | 0.0000 | SMB | 0.2247 | | 0.0641 | 3.5000 | 0.0010 |
| HML | 0.3067 | | | 0.0000 | HML | -0.0351 | | 0.0716 | | |
| MKT | 0.8224 | | | | MKT | 0.6590 | | 0.0471 | | |
| CONS | -0.0026 | 0.0032 | -0.8100 | | CONS | -0.0015 | | 0.0036 | | |
| F(3,188) | 155.0500 | | | | F(3,188) | 67.6800 | | | | |
| Prob > F | 0.0000 | | | | Prob > F | 0.0000 | | | | |
| R-squared | 0.7100 | | | | R-squared | 0.5166 | | | | |
| Adj R-squared | 0.7054 | | | | Adj R-squared | 0.5089 | | | | |
| Dependent Vari | able: R22 | | | | Dependent Varia | ble: R24 | | | | |
| | Coefficient | Std. Error | t-Statistic | Prob. | | Coefficient | Std. | Error | t-Statistic | Prob. |
| SMB | 0.2637 | | | 0.0000 | SMB | 0.4832 | | 0.0593 | | 0.0000 |
| HML | 0.0714 | | | 0.3510 | HML | -0.4813 | | 0.0662 | | |
| MKT | 0.6797 | | 13.5100 | | MKT | 0.8168 | | 0.0002 | | |
| CONS | -0.0008 | 0.0038 | -0.2200 | | CONS | 0.0020 | | 0.0430 | | 0.5490 |
| F(3,188) | 66.0600 | | | | F(3,188) | 138.4800 | | | | |
| · · · / | | | | | () | | | | | |
| Prob > F | 0.0000 | | | | Prob > F | 0.0000 | | | | |
| R-squared | 0.5105 | | | | R-squared | 0.6862 | | | | |
| Adj R-squared | 0.5028 | | | | Adj R-squared | 0.6812 | | | | |
| | | | | | | Mon | thly c | lata 1-ja | n-86 to 1-a | pr 2002 |

| Table 3B: OLS | Test of unrest | ricted Fama | and French | Model | | | | | |
|----------------|----------------|-------------|-------------|--------|---------------|-------------|---------------|--------------|----------|
| Dependent Vari | able: R31 | | | | Dependent Va | riable: R33 | | | |
| | | | | | | | | | |
| | Coefficient | Std. Error | t-Statistic | Prob. | | Coefficient | Std. Error | t-Statistic | Prob. |
| SMB | 0.1502 | 0.0699 | 2.1500 | 0.0330 | SMB | 0.2364 | 0.0505 | 4.6900 | 0.0000 |
| HML | 0.3201 | 0.0780 | 4 1000 | 0.0000 | HML | 0.0169 | 0.0563 | | 0.7640 |
| MKT | 0.9112 | | 17.7300 | | MKT | 0.7972 | | | |
| CONS | 0.0042 | 0.0039 | 1.0600 | | CONS | -0.0005 | | | |
| CONS | 0.0042 | 0.0039 | 1.0600 | 0.2690 | CONS | -0.0005 | 0.0026 | -0.1700 | 0.0010 |
| F(3,188) | 115.7600 | | | | F(3,188) | 159.6300 | | | |
| Prob > F | 0.0000 | | | | Prob > F | 0.0000 | | | |
| R-squared | 0.6464 | | | | R-squared | 0.7160 | | | |
| Adj R-squared | 0.6408 | | | | Adj R-squared | 0.7115 | | | |
| | | | | | | | | | |
| Dependent Vari | able: R32 | | | | Dependent Va | riable: R34 | | | |
| | Coefficient | Std. Error | t-Statistic | Prob. | | Coefficient | Std. Error | t-Statistic | |
| SMB | 0.4061 | 0.0619 | 6.5600 | 0.0000 | SMB | 0.3938 | 0.0757 | 5.2000 | 0.0000 |
| HML | -0.0442 | 0.0691 | -0.6400 | 0.5230 | HML | -0.2713 | 0.0845 | -3.2100 | 0.0020 |
| МКТ | 0.8892 | 0.0455 | 19.5500 | 0.0000 | MKT | 1.0170 | | | |
| CONS | -0.0021 | 0.0035 | -0.5900 | | CONS | -0.0020 | | | 0.6430 |
| | | | | | | | | | |
| F(3,188) | 137.7700 | | | | F(3,188) | 116.6300 | | | |
| Prob > F | 0.0000 | | | | Prob > F | 0.0000 | | | |
| R-squared | 0.6851 | | | | R-squared | 0.6481 | | | |
| Adj R-squared | 0.6801 | | | | Adj R-squared | 0.6425 | | | |
| naj n oquarea | 0.0001 | | | | | 0.0420 | | | |
| Dependent Vari | able: R41 | | | | Dependent Va | riable: R43 | | | |
| | Coefficient | Std. Error | t-Statistic | Prob. | | Coefficient | Std. Error | t-Statistic | Prob. |
| SMB | -0.2225 | 0.0592 | -3.7600 | 0.0000 | SMB | -0.0502 | 0.0472 | -1.0600 | 0.2890 |
| HML | 0.4408 | 0.0660 | | 0.0000 | HML | 0.0361 | | | 0.4950 |
| MKT | 0.9319 | 0.0435 | 21.4400 | | MKT | 0.9502 | | | |
| CONS | -0.0056 | 0.0033 | -1.7000 | | CONS | -0.0023 | | | |
| | 010000 | 010000 | | 0100.0 | 00110 | 0.0020 | 0.0020 | 0.0000 | 0.01.00 |
| F(3,188) | 176.9900 | | | | F(3,188) | 253.5900 | | | |
| Prob > F | 0.0000 | | | | Prob > F | 0.0000 | | | |
| R-squared | 0.7365 | | | | R-squared | 0.8002 | | | |
| Adj R-squared | 0.7323 | | | | Adj R-squared | 0.7970 | | | |
| Dependent Vari | able: R42 | | | | Dependent Va | riable: R44 | | | |
| | Coofficient | Otd Creat | t Ctotictic | Drok | - | Coofficient | Otd Creat | + Ctotioti - | Drob |
| CMD | | | t-Statistic | | CMD | Coefficient | | t-Statistic | |
| SMB | -0.2022 | 0.0431 | -4.6900 | | SMB | 0.0510 | | | 0.1160 |
| HML | 0.2445 | 0.0481 | | 0.0000 | HML | -0.1915 | | -5.3100 | |
| MKT | 0.8426 | 0.0317 | 26.5900 | | MKT | 1.0784 | | | |
| CONS | 0.0017 | 0.0024 | 0.7000 | 0.4830 | CONS | -0.0051 | 0.0018 | -2.8400 | 0.0050 |
| F(3,188) | 257.9800 | | | | F(3,188) | 693.0200 | | | |
| Prob > F | 0.0000 | | | | Prob > F | 0.0000 | | | |
| R-squared | 0.8029 | | | | R-squared | 0.9163 | | | |
| Adj R-squared | 0.7998 | | | | Adj R-squared | 0.9149 | | | |
| Auj N-squareu | 0.1990 | | | | Auj N-squaleu | | | 1-86 to 1 o | or 2002 |
| | | | | | | iviont | hly data 1-ja | 1-00 IO 1-a | µi ∠002. |

| Table 4A: GMM Test | of restricted Fama | and French Mo | del | | | | | | |
|---|--------------------------------------|----------------------------|-------------------------------------|---|--|----------------------------|-------------------|------------------|--|
| Dependent Variable: | | | | Dependent Variable: R13 | | | | | |
| Variable HML SMB MKT | 0.3710 0. | 1504 1.0564 1366 2.7166 | Prob. 0.2921 0.0072 0.0000 | Variable HML SMB MKT | Coefficient -0.0984 0.2224 0.8615 | 0.1729 0.1379 | -0.5693 1.6129 | 0.5698 0.1084 | |
| R-squared Adjusted R-squared GMM-stat p-value | 0.5755 0.5710 0.9626 0.3265 | | | R-squared Adjusted R-squared GMM-stat p-value | 0.5798 0.5754 0.0519 0.8197 | | | | |
| Dependent Variable: | R12 | | | Dependent Variable: | R14 | | | | |
| Variable HML SMB MKT R-squared Adjusted R-squared GMM-stat p-value | 0.3149 0. | 1571 0.5195 1524 2.0660 | Prob. 0.6040 0.0402 0.0000 | Variable HML SMB MKT R-squared Adjusted R-squared GMM-stat p-value | Coefficient -0.3257 0.6216 0.6577 0.3875 0.3811 0.4379 0.5082 | 0.2036 0.1488 0.0929 | -1.5997 4.1782 | | |
| Dependent Variable: | | | | Dependent Variable: | | | | | |
| Variable HML SMB MKT R-squared Adjusted R-squared GMM-stat p-value | 0.4052 0. | 1121 1.8613 0944 4.2933 | Prob. 0.0642 0.0000 0.0000 | Variable HML SMB MKT R-squared Adjusted R-squared GMM-stat p-value | Coefficient -0.1065 0.2065 0.6767 0.4991 0.4939 3.6476 0.0561 | 0.1735 0.1632 0.1126 | -0.6137 1.2652 | | |
| Dependent Variable: | R22 | | | Dependent Variable: | R24 | | | | |
| Variable HML SMB MKT | 0.2250 0. | 1147 0.5887 1064 2.1147 | Prob. 0.5568 0.0358 0.0000 | Variable HML SMB MKT | Coefficient -0.4838 0.4615 0.8134 | 0.0929 0.0684 | -5.2103 6.7513 | 0.0000 0.0000 | |
| R-squared Adjusted R-squared GMM-stat p-value | 0.4997 0.4945 2.5412 0.1109 | | | R-squared Adjusted R-squared GMM-stat p-value | 0.6828 0.6795 0.9202 0.3374 Month | | n-86 to 1-₂ | upr 2002 | |

| Table 4B: GMM Test | | ama and F | rench Moo | del | | 500 | | | | |
|---------------------|-------------|------------|-------------|--------|-------------------------|-------------|--------------|-------------|--------|--|
| Dependent Variable: | R31 | | | | Dependent Variable: R33 | | | | | |
| Variable | Coefficient | Std. Error | t-Statistic | Prob. | Variable | Coefficient | Std. Error | t-Statistic | Prob. | |
| HML | 0.3546 | 0.1922 | 1.8447 | 0.0666 | HML | -0.0342 | 0.1279 | -0.2676 | 0.7893 | |
| SMB | 0.1180 | 0.1181 | | 0.3188 | SMB | 0.2098 | | | 0.0575 | |
| MKT | 0.9078 | 0.0703 | | | MKT | 0.7817 | | | 0.0000 | |
| | 0.3070 | 0.0705 | 12.9000 | 0.0000 | WIXT | 0.7017 | 0.0012 | 9.0225 | 0.0000 | |
| R-squared | 0.6476 | | | | R-squared | 0.7066 | | | | |
| Adjusted R-squared | 0.6440 | | | | Adjusted R-squared | 0.7035 | | | | |
| GMM-stat | 0.1842 | | | | GMM-stat | 4.5537 | | | | |
| p-value | 0.6678 | | | | p-value | 0.0328 | | | | |
| Dependent Variable: | R32 | | | | Dependent Variable: | R34 | | | | |
| Variable | Coefficient | Std. Error | t-Statistic | Prob. | Variable | Coefficient | Std. Error | t-Statistic | Prob. | |
| HML | -0.1788 | 0.0975 | -1.8345 | | HML | -0.3064 | | | | |
| SMB | 0.3581 | 0.1144 | | 0.0020 | SMB | 0.3458 | | | 0.0352 | |
| мкт | 0.8980 | 0.0907 | | 0.0000 | MKT | 1.0576 | | | 0.0000 | |
| | 0.0300 | 0.0307 | 9.9000 | 0.0000 | WIXT | 1.0070 | 0.1120 | 9.5725 | 0.0000 | |
| R-squared | 0.6661 | | | | R-squared | 0.6376 | | | | |
| Adjusted R-squared | 0.6627 | | | | Adjusted R-squared | 0.6338 | | | | |
| GMM-stat | 5.1482 | | | | GMM-stat | 3.6086 | | | | |
| p-value | 0.0233 | | | | p-value | 0.0575 | | | | |
| | | | | | | | | | | |
| Dependent Variable: | | | | | Dependent Variable: | | | | | |
| Variable | Coefficient | Std. Error | t-Statistic | Prob. | Variable | Coefficient | Std. Error | t-Statistic | Prob. | |
| HML | 0.4782 | 0.1131 | 4.2284 | 0.0000 | HML | 0.1300 | 0.1097 | 1.1855 | 0.2373 | |
| SMB | -0.3833 | 0.1043 | -3.6759 | 0.0003 | SMB | -0.2274 | 0.0910 | -2.4981 | 0.0133 | |
| МКТ | 0.9634 | 0.0637 | 15.1285 | 0.0000 | MKT | 0.9455 | 0.0550 | 17.1812 | 0.0000 | |
| R-squared | 0.7078 | | | | R-squared | 0.7812 | | | | |
| Adjusted R-squared | 0.7048 | | | | Adjusted R-squared | 0.7789 | | | | |
| GMM-stat | 8.0599 | | | | GMM-stat | 7.7432 | | | | |
| p-value | 0.0045 | | | | p-value | 0.0054 | | | | |
| Dependent Variable: | R42 | | | | Dependent Variable: | R44 | | | | |
| Variable | Coefficient | Std. Error | t-Statistic | Prob. | Variable | Coefficient | Std. Error | t-Statistic | Prob. | |
| HML | 0.2087 | 0.0802 | 2,6015 | 0.0100 | HML | -0.1785 | | | | |
| SMB | -0.2233 | 0.0637 | | 0.0006 | SMB | 0.0342 | | | 0.4650 | |
| МКТ | 0.8743 | | 14.2658 | | MKT | 1.0126 | | | | |
| R-squared | 0.7940 | | | | R-squared | 0.8961 | | | | |
| Adjusted R-squared | 0.7918 | | | | Adjusted R-squared | 0.8950 | | | | |
| GMM-stat | 2.1232 | | | | GMM-stat | 16.3914 | | | | |
| p-value | 0.1451 | | | | p-value | 0.0001 | | | | |
| p-value | 0.1401 | | | | p-value | | y data 1-jar | 00 1- 1 - | 0000 | |

| Table 5: GMM Test of | f unrestricted | Fama and | French Mc | del | | | | | |
|----------------------|----------------|------------|-------------|--------|---------------------|-------------|---------------|-------------|----------|
| Dependent Variable: | R12 | | | | Dependent Variable: | R21 | | | |
| Variable | Coefficient | Std. Error | t-Statistic | Prob. | Variable | Coefficient | Std. Error | t-Statistic | Prob. |
| HML | 0.0888 | 0.1626 | 0.5460 | 0.5857 | HML | 0.3151 | 0.1046 | 3.0122 | 0.0029 |
| SMB | 0.3767 | 0.1556 | 2.4210 | 0.0164 | SMB | 0.3971 | 0.0927 | 4.2839 | 0.0000 |
| МКТ | 0.7899 | | | 0.0000 | MKT | 0.8178 | | | |
| C | -0.0083 | | -2.3154 | | C | -0.0083 | | | |
| R-squared | 0.5833 | | | 0.02 | R-squared | 0.7062 | | | 0.0000 |
| Adjusted R-squared | 0.5767 | | | | Adjusted R-squared | 0.7016 | | | |
| GMM-stat | 0.0000 | | | | GMM-stat | 0.0000 | | | |
| p-value | 1.0000 | | | | p-value | 1.0000 | | | |
| p-value | 1.0000 | | | | p-value | 1.0000 | | | |
| Dependent Variable: | R32 | | | | Dependent Variable: | R33 | | | |
| Variable | Coefficient | Std. Error | t-Statistic | Prob. | Variable | Coefficient | Std. Error | t-Statistic | Prob. |
| HML | -0.0358 | | | 0.7695 | HML | 0.0253 | | | 0.8374 |
| SMB | 0.3997 | | | 0.0036 | SMB | 0.2300 | | | 0.0308 |
| MKT | 0.8846 | | | 0.0000 | MKT | 0.7927 | | | |
| C | -0.0077 | | | 0.0076 | C | -0.0061 | | | |
| R-squared | 0.6830 | | -2.0330 | 5.0070 | R-squared | 0.7154 | | -2.0000 | 0.0207 |
| Adjusted R-squared | 0.6780 | | | | Adjusted R-squared | 0.7154 | | | |
| | | | | | | | | | |
| GMM-stat | 0.0000 | | | | GMM-stat | 0.0000 | | | |
| p-value | 1.0000 | | | | p-value | 1.0000 | | | |
| Dependent Variable: | R41 | | | | Dependent Variable: | R43 | | | |
| Variable | Coefficient | Std. Error | t-Statistic | Prob. | Variable | Coefficient | Std. Error | t-Statistic | Prob. |
| HML | 0.449145 | 0.133313 | 3.3691 | 0.0009 | HML | 0.0444 | | | 0.7005 |
| SMB | | 0.122422 | -1.8695 | | SMB | -0.0566 | | | |
| MKT | | 0.060306 | 15.3782 | | MKT | 0.9456 | | 15.4695 | |
| C | | 0.003328 | | | C | -0.0080 | | | |
| R-squared | 0.732525 | | 0.00000 | 0.0000 | R-squared | 0.8025 | | 0.2002 | 0.0014 |
| Adjusted R-squared | 0.728302 | | | | Adjusted R-squared | 0.7994 | | | |
| GMM-stat | 0.720302 | | | | GMM-stat | 0.0000 | | | |
| | | | | | | | | | |
| p-value | 1.0000 | | | | p-value | 1.0000 | | | |
| Dependent Variable: | R44 | | | | | | | | |
| Variable | Coefficient | Std. Error | t-Statistic | Prob. | | | | | |
| HML | -0.183155 | 0.060546 | -3.02507 | 0.0028 | | | | | |
| SMB | | 0.046995 | | | | | | | |
| MKT | | 0.036832 | | 0.0400 | | | | | |
| C | | 0.001972 | | 0 | | | | | |
| R-squared | 0.913824 | | 0.40000 | U | | | | | |
| Adjusted R-squared | 0.913824 | | | | | | | | |
| GMM-stat | 0.912403 | | | | | | | | |
| | | | | | | | | | |
| p-value | 1.0000 | | | | | | | | |
| | | | | | | | | | |
| | | | | | | Month | nly data 1-ja | n-86 to 1-a | apr 2002 |
| L | | | | | | | , j | | |

| Table 6: GMM Test of | restricted Fa | ama and Fre | ench Mode | I with WML Factor | | | | | |
|-----------------------|---------------|-------------|-------------|-------------------|---------------------|-------------|--------------|-------------|---------|
| Dependent Variable: | | | | | Dependent Variable: | R21 | | | |
| Variable | Coefficient | Std. Error | t-Statistic | Prob. | Variable | Coefficient | Std. Error | t-Statistic | Prob. |
| HML | 0.0877 | 0.1486 | 0.5899 | 0.5560 | HML | 0.2202 | 0.1013 | 2.1733 | 0.0310 |
| SMB | 0.3349 | | | 0.0235 | SMB | 0.4081 | 0.0879 | 4.6425 | 0.0000 |
| MKT | 0.7803 | | | 0.0000 | MKT | 0.8393 | | | |
| WML | -0.0512 | | -0.8227 | | WML | -0.0561 | | | |
| R-squared | 0.5745 | | -0.0221 | 0.4117 | R-squared | 0.6970 | | -1.0040 | 0.2002 |
| Adjusted R-squared | 0.5678 | | | | Adjusted R-squared | 0.6922 | | | |
| GMM-stat | 4.9340 | | | | GMM-stat | 6.1880 | | | |
| | | | | | | | | | |
| p-value | 0.0263 | | | | p-value | 0.0128 | | | |
| Dependent Variable: I | R32 | | | | Dependent Variable: | R33 | | | |
| Variable | | Std. Error | t-Statistic | Prob. | Variable | Coefficient | Std. Error | t-Statistic | Prob. |
| HML | -0.1751 | 0.0949 | -1.8452 | | HML | -0.0321 | | | |
| SMB | 0.3640 | | | 0.0017 | SMB | 0.2163 | | | 0.0445 |
| MKT | 0.9030 | | 10.0364 | | MKT | 0.7855 | | | 0.0000 |
| WML | -0.0241 | | -0.5756 | | WML | -0.0226 | | | 0.6239 |
| R-squared | 0.6675 | | -0.5750 | 0.0000 | R-squared | 0.7091 | | -0.4312 | 0.0200 |
| | 0.6623 | | | | | 0.7091 | | | |
| Adjusted R-squared | | | | | Adjusted R-squared | | | | |
| GMM-stat | 5.2960 | | | | GMM-stat | 4.7830 | | | |
| p-value | 0.0213 | | | | p-value | 0.0287 | | | |
| Dependent Variable: I | R41 | | | | Dependent Variable: | R43 | | | |
| Variable | Coefficient | Std. Error | t-Statistic | Prob. | Variable | Coefficient | Std. Error | t-Statistic | Prob. |
| HML | 0.4880 | | | 0.0000 | HML | 0.1310 | | | 0.2302 |
| SMB | -0.3849 | | -3.6885 | | SMB | -0.2314 | | | |
| MKT | 0.9651 | 0.0633 | 15.2373 | | MKT | 0.9494 | | | |
| WML | -0.0112 | | -0.3869 | | WML | -0.0238 | | | |
| R-squared | 0.7080 | | 0.0000 | 0.000L | R-squared | 0.7822 | | 0.0002 | 5.0000 |
| Adjusted R-squared | 0.7080 | | | | Adjusted R-squared | 0.7822 | | | |
| GMM-stat | 8.1370 | | | | GMM-stat | 7.9760 | | | |
| | | | | | | | | | |
| p-value | 0.0043 | | | | p-value | 0.0047 | | | |
| Dependent Variable: I | R44 | | | | | | | | |
| Variable | Coefficient | Std. Error | t-Statistic | Prob. | | | | | |
| HML | -0.1685 | 0.0477 | -3.5316 | 0.0005 | | | | | |
| SMB | 0.0347 | 0.0417 | 0.8303 | 0.4074 | | | | | |
| MKT | 1.0074 | 0.0359 | 28.0336 | 0.0000 | | | | | |
| WML | 0.0379 | | | 0.0020 | | | | | |
| R-squared | 0.8992 | | | | | | | | |
| Adjusted R-squared | 0.8976 | | | | | | | | |
| GMM-stat | 16.1320 | | | | | | | | |
| p-value | 0.0000 | | | | | | | | |
| F | 0.000 | | | | | | | | |
| | | | | | | | | | |
| | | | | | | Month | y data 1-jar | n-86 to 1-a | pr-2002 |